## MTH 203, Calculus III, Quiz One Spring 2013

Ayman Badawi

QUESTION 1. Find an equation of the plane that passes through the points $(1,-1,2),(-1,1,4)$ and $(1,1,3)$. Does the vector $i-3 j+k$ lie in such plane? explain.

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.
E-mail: abadawi@aus.edu, www.ayman-badawi.com

## MTH 203, Calculus III, Quiz One Spring 2013

Ayman Badawi

QUESTION 1. Given $Z=f(x, y)=x^{2} e^{x y}+\ln (x y+7)+y^{3}-x^{2}+3 x y$
a) Find the domain of $f(x, y)$. Does $f(x, y)$ represent a curve or a solid object in 3D?
b) Find $f_{x}=d z / d x$

QUESTION 2. Given $e^{z x}+x z+y^{3} z-3 z x y+7=0$.
a) Find $d z / d x$. Then evaluate $d z / d x$ when $x=0$ and $z=1$.
b) Find $d y / d x$ and evaluate $d y / d x$ when $y=2$ and $x=0$

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.
E-mail: abadawi@aus.edu, www.ayman-badawi.com

## MTH 203, Calculus III, Quiz three Spring 2013

Ayman Badawi

QUESTION 1. Find the volume of the object that has a base on the xy-plane, say $D$, where $D$ is the region in the first quadrant and it is bounded by the two functions $y=x^{2}$ and $y=x$. The height is $z$ which is a function in terms of x and $\mathrm{y}, z=f(x, y)=e^{\left(y^{1.5}-0.75 y^{2}+1\right)}$.

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.
E-mail: abadawi@aus.edu, www.ayman-badawi.com

## MTH 203, Calculus III, Quiz four Spring 2013

Ayman Badawi

QUESTION 1. Find the surface area of the part of the surface $z=x+y^{2}$ that lies above the triangular region in the $x y$-plane with vertices $(0,0),(2,0)$ and $(2,1)$.

QUESTION 2. Find the volume of the object with base $x^{2}+y^{2}=3$ and height $z=\sqrt{1+x^{2}+y^{2}}$

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.

## MTH 102, Calculus for Business, Quiz three, Spring 2013

Ayman Badawi

QUESTION 1. Find $f^{\prime}(x)$ and do not simplify:
${ }_{\text {a) }} f(x)=2 \sqrt{4 x+1}-\frac{7}{5 x-3}+\frac{3}{x}+10$
b) $f(x)=(3 x+7)\left(2 x^{2}-5 x+1\right)^{8}$

QUESTION 2. Let $x$ be number of units of a certain product in hundreds and

$$
P(x)=\sqrt{x^{2}-8 x+17}
$$

be the profit function in hundred of DHS.
a) Find $P(5)$ and $P(6)$.
b) Find the marginal profit when $x=5$
c) Relate the answer in (b) to part (a). i.e., write a statement that is so clear for a reader.

## MTH 203, Calculus III, Quiz 6 Spring 2013

Ayman Badawi

QUESTION 1. Find the area of the part that is bounded by $f(x, y)=e^{\left(x^{2}+y^{2}+4\right)}$ and the circle (in the xy- plane) $x^{2}+y^{2}=9$

QUESTION 2. A force vector function $F(x, y)=2 y i+6 x j$ is applied on a particle that moves from $(2,0)$ (counter clockwise) and then back to the same point $(2,0)$ along the circle $x^{2}+y^{2}=4$. Find the work.

## Faculty information

## MTH 203, Calculus III, Quiz 6 Spring 2013

Ayman Badawi

QUESTION 1. The path of a plane AA is the line $L_{1}: x=5+2 t, y=-8+t, z=12+4 t$. The path of a plane BB is the line $\mathrm{F}: x=5 s, y=-13+3 s, z=2+10 s$. Show that the two planes pass through a unique point in space and find the coordinates of this point. Will the two planes collapse in space?

QUESTION 2. Find the distance between the point $(2,2,2)$ and the line $L: x=3 t, y=4 t, z=1$

QUESTION 3. Let $V=2 i+j-10 k, U=6 i+6 j+3 k$. Find $\operatorname{Proj}_{U}^{V}$ and $\left|\operatorname{Proj} j_{U}^{V}\right|$. Roughly sketch the three vectors $U, V$ and $\operatorname{Proj}_{U}^{V}$.

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.
E-mail: abadawi@aus.edu, www.ayman-badawi.com

# MTH 203, Calculus III, Quiz 7 Spring 2013 

Ayman Badawi

QUESTION 1. Let $f(t)=<\sqrt{t-3}, t+1, \sin (\sqrt{t-3})>$
) a) Find the domain of $f(t)$
b) Find the domain of $f$ in the $x y$-plane. Sketch the domain in the xy-plane
c) Describe all points in the $x y$-plane where the curve of $f$ intersects the xy-plane.
d) Find a point on the curve of $f$ where the tangent line to the curve at that point is horizontal (i.e., horizontal here means it does not intersect the $x y$ plane, there are infinitely many points, just give me one)).
e) Find a parametric equations of the tangent line to the curve of $f$ at the point $(1,5, \sin (1))$.

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.
E-mail: abadawi@aus.edu, www.ayman-badawi.com

## MTH 203, Calculus III, Quiz 8 Spring 2013

Ayman Badawi

QUESTION 1. Given $f(x, y)=18 x+5 y+x^{2}-2 x y+1$ defined on the closed region that is bounded by $y=x^{2}$ and $y=16$. Find the absolute minimum and the absolute maximum of $f(x, y)$ over the given closed region.

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.
E-mail: abadawi@aus.edu, www.ayman-badawi.com

## MTH 111, Math for Architects, Quiz 10 Spring 2013

Ayman Badawi

QUESTION 1. Given the points: $A=(2,4)$ and $B=(0,2)$. Find a point $C$ on the x -axis so that $|A C|+|C B|$ is minimum. You need to find the coordinates of the point $C$.

## Faculty information

Ayman Badawi, Department of Mathematics \& Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.
E-mail: abadawi@aus.edu, www.ayman-badawi.com

